

7-3

Elimination Using Addition and Subtraction

(Pages 382–386)

In systems of equations where the coefficients of terms containing the same variable are *opposites*, the **elimination** method can be applied by adding the equations. If the coefficients of those terms are the *same*, the elimination method can be applied by subtracting the equations.

Examples Solve each system of equations using elimination.

a. $x - 2y = 13$ and $3x + 2y = 15$

Add the two equations, since the coefficients of the y -terms, -2 and 2 , are opposites.

$$\begin{array}{r} x - 2y = 13 \\ (+) 3x + 2y = 15 \\ \hline \end{array}$$

$$4x = 28 \quad \text{Solve for } x.$$

$$x = 7 \quad \text{Divide each side by 4.}$$

$$x - 2y = 13 \quad \text{Use the first equation.}$$

$$7 - 2y = 13 \quad \text{Substitute 7 for } x.$$

$$-2y = 6 \Rightarrow y = -3$$

The solution of the system is $(7, -3)$.

b. $3x + 4y = 5$ and $3x - y = -5$

Subtract the two equations, since the coefficients of the x -terms are the same.

$$\begin{array}{r} 3x + 4y = 5 \\ (-) 3x - y = -5 \\ \hline \end{array}$$

$$5y = 10 \quad \text{Solve for } y.$$

$$y = 2 \quad \text{Divide each side by 5.}$$

$$3x - y = -5 \quad \text{Use the second equation.}$$

$$3x - 2 = -5 \quad \text{Substitute 2 for } y.$$

$$3x = -3 \Rightarrow x = -1$$

The solution of the system is $(-1, 2)$.

Try These Together

State whether addition, subtraction, or substitution would be most convenient to solve each system of equations. Then solve the system.

1. $x - y = 3$

$$3x + y = 1$$

2. $3x + 4y = 2$

$$2x + 4y = 8$$

3. $2x + 4y = 8$

$$y - 3 = x$$

Practice

State whether addition, subtraction, or substitution would be most convenient to solve each system of equations. Then solve the system.

4. $x + 2y = 3$

$$-x + y = 6$$

5. $x + y = -2$

$$x - y = 8$$

6. $2y - 3x = 12$

$$-2y + 6x = -5$$

7. $2x + y = -5$

$$x + 3y = 25$$

8. $x - 4y = 16$

$$2x - 4y = 18$$

9. $2x + 4y = 6$

$$3x - 4y = 2$$

10. $8x + y = 1$

$$-8x - 4y = 3$$

11. $2x - 5y = -6$

$$2x + 3y = -9$$