

5. Review of exponents: Recall that

$x^4 \rightarrow$ “ x to the fourth power” means “4 factors of x ”

$3^4 \rightarrow$ “3 to the fourth power” means “4 factors of 3”

$$3^4 = 3 \cdot 3 \cdot 3 \cdot 3$$

$$= 81$$

a. 10^3 means “_____ factors of _____,” therefore, $10^3 =$ _____.

b. 2^4 means “_____ factors of _____,” therefore, $2^4 =$ _____.

c. 9^2 means “_____ factors of _____,” therefore, $9^2 =$ _____.

6. One of the Laws of Exponents tells us that $\frac{x^a}{x^b} = x^{a-b}$.

- This means that when you divide two expressions that have the same variable, you **subtract the exponents**.

- Therefore, $\frac{x^7}{x^2} = x^5$ and $\frac{x^4}{x^1} = x^3$

Use this Law of Exponents to write an equivalent expression for the following quotients:

a. $\frac{x^9}{x^5} =$ _____

b. $\frac{x^{24}}{x^{11}} =$ _____

c. $\frac{x^6}{x^5} =$ _____

7. A long time ago you learned that any time you divide a number by itself, the quotient is 1:

$$\frac{4}{4} = 1, \quad \frac{-13}{-13} = 1, \quad \text{and} \quad \frac{212}{212} = 1.$$

The same result happens even when you divide a variable (with an exponent) by itself:

$$\frac{x^9}{x^9} = 1, \quad \frac{x^2}{x^2} = 1, \quad \text{and} \quad \frac{x^6}{x^6} = 1.$$

But remember, the Law of Exponents that we used in question 6 (above) also tells us that when we are dividing the same variable, we can subtract the exponents to create an equivalent expression. So now we can say the following:

- Using that Law of Exponents, we know that $\frac{x^9}{x^9} = x^0 \rightarrow$ but we also know that $\frac{x^9}{x^9} = 1$

- Using that Law of Exponents, we know that $\frac{x^2}{x^2} = x^0 \rightarrow$ but we also know that $\frac{x^2}{x^2} = 1$

- Using that Law of Exponents, we know that $\frac{x^6}{x^6} = x^0 \rightarrow$ but we also know that $\frac{x^6}{x^6} = 1$

a. **Complete the following sentence:** Based on the information above, I can conclude that $x^0 =$ _____. In other words, anything to the zero power will always equal _____.